# **Model calibration**

# Composite <u>Global Ply</u> model 131 for elastic, damage and failure

- PAM-CRASH material model 131 is for multi-layered composite shell elements.
- Within this model different ply types can be used for different fibre reinforcements and damage laws. This document covers the ESI composite <u>Global Ply</u> damage law for:
  - 1. Ply type 1 for uni-directional composites (shell elements only).
  - 2. Ply type 7 for woven type composites (shell elements only).
- The Global Ply law is not available for solid elements.

#### **Problem description**

Outline	Application of the 'Global Ply' composite damage model to a single element under various loadings
Analysis type(s):	Explicit
Element type(s):	Applicable to shell elements (material model 131)
Materials law(s):	<ul><li>PAM-CRASH material model 131 (composite ply types 1 and 7).</li><li>Fibre and matrix are calibrated for:</li><li>1) Orthotropic elasticity</li><li>2) Orthotropic fibre and matrix damage with failure</li></ul>
Model options:	Boundary conditions, Imposed velocity loads, Composite materials
Key results:	Outputs for composites (fibre stresses and strains, matrix damage, fibre orientations )
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#### **Background information**

#### Pre-processor, Solver and Post-processor used:

- Visual-Crash PAM: To assign material, loading, constraint and control data.
- Analysis (PAM-CRASH Explicit): To perform the explicit Finite Element analysis.
- Visual-Viewer: To evaluate results for contour plots, stresses and strains, etc.

#### Prior knowledge for the exercise

It is assumed the user has some knowledge of Visual-Crash PAM and PAM-CRASH.

#### **Problem data and description**

Units: kN, mm, kg, ms

Description: Single shell element 10mm \* 10mm and 1mm thick

Loading: Imposed constant velocity at 1mm/msec (duration of study 1msec)  $\Rightarrow$  total displacement 1mm and strain 0.1 (= 10%)

#### Loading cases:



Case 1: Axial fibre

Case 2: Transverse matrix Case 3: Shear loading

Material: The material to be analysed is a high performance balanced woven fabric composite. The data is presented from mechanical testing in the exercise.

#### **Supplied datasets**

All completed datasets are supplied. The main aim is to demonstrate the strategy for model calibration which is done here using the shell element (material model 131, ply type 1).

#### Calibration for orthotropic elastic properties:

Fibre direction in tension	Ply1_TensionX_Elastic.pc
Fibre direction in compression	Ply1_CompressionX_Elastic.pc
Shear loading	Ply1_ShearXY_Elastic.pc

#### Calibration for damage, plasticity and failure:

Fibre direction in tension (fibre failure)	Ply1_TensionX_ElasticFibreFailure.pc
Fibre direction in compression (fibre fa	ilure) Ply1_CompressionX_ElasticFibreFailure.pc
Shear loading (elasto-plastic shear)	Ply1_ShearXY_ElasticDamageFailure_Option1_Plastic.pc
Shear loading (elasto-plastic shear)	Ply1_ShearXY_ElasticDamageFailure_Option2_Plastic.pc
Shear loading (elasto-plastic shear)	Ply1_ShearXY_ElasticDamageFailure_Option3_Plastic.pc
Cyclic loading (elasto-plastic shear)	Ply1_ShearXY_ElasticDamageFailure_Option3_Plastic_Cyclic.pc

#### Comments concerning ply types 1 and 7

Two ply types are available that use the Global ply damage law for UD and woven type composites:

- Ply type 1 is intended for UD composites, but can also be used to approximate a woven fabric by stacking two UD layers with appropriate fibre angles and distribution of mechanical properties. Indeed, it can be advantageous for non-orthogonal reinforcement (e.g. ±30°) and cases where large intra-ply shear strains occur.
- Ply type 7 is for woven fabrics and mostly suited to orthogonal reinforcement and applications where shear strains are small. The following table summarises these three cases.

Option / Ply type	Representation	Comments
1 (Ply type 1)	t\$	Standard representation for UD composite plies
2 (Two layers of Ply type 1)		<ul> <li>The woven composite is idealised as two stacked plied of ply type 1</li> <li>In plane and shear properties must be carefully distributed between plies</li> <li>Useful for non-orthogonal reinforcement and large shear loading</li> </ul>
3 (Ply type 7)		<ul><li>Standard representation for woven composite plies:</li><li>Ideally for orthogonal reinforcement</li><li>Intra-ply shear strains should not be large</li></ul>

This document demonstrates the calibration strategy for option 2 in the above table applied to a 'balanced' woven fabric composite. Actual tests results are used in this calibration. The methods used are identical if standard ply types 1 or 7 are used.

#### **Basic theory**

A full description of the Global ply model is given in the original reference<sup>1</sup> and also in the ESI PAM-CRASH<sup>TM</sup> user's manual<sup>2</sup>.

Essentially the fibre phase uses a strain based failure criteria for tension and compression; non-linear (elastic) behaviour is possible in compression and is often necessary to account for micro-buckling effects in compression. The shear behaviour uses a coupled damage and plasticity model that accounts for modulus reduction and permanent plastic deformations. The fibre and matrix laws are decoupled, but parameters are available that allow coupling of transverse and shear matrix damage.

<sup>&</sup>lt;sup>1</sup> Ladevèze P, Le Dantec E, "Damage Modelling of the elementary ply for laminated composites", Composites Science and Technology, Vol. 43, Issue 3, 1992, pp. 257-267.

<sup>&</sup>lt;sup>2</sup> PAM-CRASH<sup>™</sup> Users manuals, Engineering Systems International, 20 Rue Saarinen, Silic 270, 94578 Rungis-Cedex, France. <u>www.esi-group.com</u>

#### Part 1: Some basic explanation of the input data

Typical model loadings and supports (e.g. for dataset Ply1\_TensionX\_Elastic.pc)

Load the dataset into the Visual-Crash Program (VCP) and study the supports and the loading:

- 1. In Loads > Displacement Boundary Condition the following definitions are found:
  - Node 1 is fully constrained.
  - Node 2 is fully fixed, except free in the x-direction.
  - Node 4 is fully fixed, except free in the y-direction.
- In Loads > 3D BC nodes 2 and 3 are loaded at constant velocity in the positive x-direction (for tension fibre loading).
- **Remark:** This simple setup ensures the element is properly supported and has pure tension loading in the x-direction with free contraction in the y-direction.

#### Ply, Material and Part data cards

#### Note from the dataset:

- 1. **The parts** data contain information on geometric data such as the reference fiber orientation. A link to associated material data (variable **IMAT**) is also made.
- 2. **The materials** cards (**IMAT**) contain information on density, the number of plies in the laminate and the stacking sequence. Within this stacking sequence information on each ply, including the reference ply set (parameter **IDPLY**), the ply thickness and a fibre orientation angle are defined.
- 3. The ply cards (IDPLY) contain all ply mechanical data for stiffness, damage and failure.

Considering the sequence in which the data refers to each other  $(1 \rightarrow 2 \rightarrow 3)$  it is best to define things in reverse order; i.e. the plies first, then materials and finally parts; all three are needed.

Ply Creation/Editir

#### Ply cards

(e.g. Ply properties for dataset Ply1 TensionX Elastic.pc).

In the ply cards you will find the mechanical, damage and failure data assigned to the ply.

- IDPLY is the ply identification number and ITYP is the ply type (1 or 7).
- o The mechanical data (density, modulus, shear and Poison's ratio) are given on the first cards. This is then followed by failure, compression, plasticity and strain rate data.
- Note: Contrary to the PAM-CRASH Bi-phase model all mechanical data represents homogenised properties.

#### Material cards

(e.g. Material properties for dataset Ply1\_TensionX\_Elast

- 1. The number of plies in the laminate are defined (NOPLY) and for each ply the associated ply number (IDPLY), the ply thickness (THKPL) and fibre angle (ANGPL) are defined. Note the fibre angle is with respect to a reference vector defined in the Parts cards (see below) and that two stacked plies are defined.
- 2. Special output results to the .THP and .DSY files (or .ENF file if used) are possible such as fiber, transverse and shear stresses/strains. For this the ply number in the laminate lay-up and an auxiliary reference number for the variable to be output are given. Examples of auxiliary reference numbers are

_								
			Visible	🗹 Highlight	Show	Reset	Apply (	Close
ic	.pc).							
	Material Ed	litor						
	ID: 1 \$510	Elemen 520530-	t Type: All(Str. 54055	uct) 🔽 Typ 05605	e: 131-MUL1 70580	TILAYERED	ORTHOTR	OPIC,
	MATER /	1	1	<b>•</b>	1	1	1	1
	MATER / BLANK	IDMAT 1 AUXID1	MATYP 131 AUXID2	RHO 1.8E-6 AUXID3	ISINT 0 AUXID4	ISHG 0 AUXID5	ISTRAT AUXID6	IFR QV
	NAME KSI	U TITLE UD ply Fo	NOPLY	IMETHOD	HGM	HGW	HGQ	As
	0.1 IDPLY 1	0. THKPL 0.5	2 ANGPL 0.					
	BLANK	NMIN 0	BLANK	GRUC_KW	GRUC_VAL	IFAIL 0	BLANK	ER/
	IDPLY1	IDAUX1	IDPLY2	IDAUX2	IDPLY3	IDAUX3	IDPLY4	IDA
	IDPLY9		1 IDPL ¥40		IDPL V11		IDPL V12	
	2	3	2	6	2	7	2	8
	IDPLY17	IDAUX17	IDPLY18	IDAUX18	IDPLY19	IDAUX19	IDPLY20	IDA
	IDPLY25	IDAUX25	IDPLY26	IDAUX26	IDPLY27	IDAUX27	IDPLY28	IDA

Aux's 1-3 for fibre strain11, strain22 and shear strain12, and Aux's 6-8 for corresponding fiber stresses. Auxiliary reference numbers are also available for results such as fibre and matrix damage.

#### Part cards

(e.g. Part properties for dataset Ply1 TensionX Elastic.pc).

- 1. The connection to the associated material is made via the **IDMAT** number (in this case = 1).
- 2. A vector for the reference fibre direction is defined. Here the global vector option with a reference vector 1,0,0 (i.e. the global x-direction) is used. For shell elements the transverse direction is normal to the fiber direction in the element plane.





## Part 2: Determination of orthotropic elastic and failure properties from test measurements

In this exercise test results are first presented from which the necessary material properties for stiffness and failure are extracted. The model and input data are then validated using a single element test case.

For the woven fabric composite the tests needed to extract data are:

- 1. Tension test on  $0^{\circ}$  specimens  $\Rightarrow$  elastic and failure properties
- 2. Compression test on  $0^{\circ}$  specimens  $\Rightarrow$  elastic and failure properties
- 3a. Shear elastic properties (Tension test on a ±45° specimen)
- 3b. Shear damage properties (Cyclic tension test on a ±45° specimen)
- 3c. Shear plasticity properties (Cyclic tension test on a ±45° specimen)

#### 1. Tension test on 0° specimens: Elastic and failure properties

Four test coupons loaded in the 0° direction (=90° direction for a balanced woven fabric composite) are shown. For a simple coupon:

$$\begin{cases} \boldsymbol{\sigma}_{11} \\ \boldsymbol{\sigma}_{22} \\ \boldsymbol{\sigma}_{12} \end{cases} = \begin{cases} \boldsymbol{\sigma}_{L} \\ \boldsymbol{0} \\ \boldsymbol{0} \end{cases} \text{ and } \begin{cases} \boldsymbol{\varepsilon}_{11} \\ \boldsymbol{\varepsilon}_{22} \\ 2\boldsymbol{\varepsilon}_{12} \end{cases} = \begin{cases} \boldsymbol{\varepsilon}_{L} \\ \boldsymbol{\varepsilon}_{T} \\ \boldsymbol{0} \end{cases}$$

by definition  $\sigma_L = E_1^{0t} \varepsilon_L \Rightarrow E_1^{0t} = \frac{\sigma_L}{\varepsilon_L}$ 



There is some scatter in the test data; but reasonable averages for stiffness and failure data are summarised in the table below.

Property	Value
$E_1^{0t}$ Tensile elastic modulus (fibre direction)	67.5 GPa
$\sigma_{i}^{ft}$ Tensile failure stress (fibre direction)	880 MPa
$\mathcal{E}_{i}^{f}$ Tensile failure strain (fibre direction) - initiation	0.013
$\mathcal{E}_{u}^{f}$ Tensile failure strain (fibre direction) - ultimate	0.0131
$d_u^{ft}$ Assumed ultimate damage (fibre direction)	1.0

#### 2. Compression test on 0° specimens: Elastic and failure properties

In this case  $E_1^{0C}$  is given by the initial slope of the compression stress-strain curve (dashed line); e.g.





All other failure data is estimated and given in the table below.

Property	Value
$E_1^{0t}$ Compression elastic modulus (fibre direction)	69.0 GPa
$\sigma_{i}^{ft}$ Compression failure stress (fibre direction)	650 MPa
$\mathcal{E}_i^{fi}$ Compression failure strain (fibre direction) - initiation	0.0104
$\mathcal{E}_{u}^{ft}$ Compression failure strain (fibre direction) - ultimate	0.0105
$d_u^{ft}$ Ultimate compression damage (fibre direction)	1.0

A further useful parameter in compression is the corrective parameter ( $\gamma$ ) to help approximate the nonlinear compression curve (due to fibre crimp and micro-buckling). This is given by,

$$\begin{split} E_1^{0c} &= \text{intial slope of the curve} \\ \gamma &= \frac{E_1^{0c} - E_1^{\gamma}}{E_1^{\gamma} E_1^{0c} |\epsilon_{11}|} \end{split}$$

Performing this computation about an arbitrary point (e.g. strain  $\epsilon_{11} = 0.008$ ) gives  $\underline{y} = 0.17$ 

#### 3a. Shear elastic properties (Tension test on a ±45° specimen)

For the elastic shear data the initial (undamaged) portion of the tensile loaded cyclic shear test is used; an example for the woven fabric is given below. The stress-strain relations in the fibre frame are defined as follow:

$$\begin{cases} \sigma_{11} \\ \sigma_{22} \\ \sigma_{12} \end{cases} = \begin{cases} 0 \\ 0 \\ \sigma_L / 2 \end{cases} \text{ and } \begin{cases} \varepsilon_{11} \\ \varepsilon_{22} \\ 2\varepsilon_{12} \end{cases} = \begin{cases} 0 \\ 0 \\ \varepsilon_L - \varepsilon_T \end{cases}$$

 $G_{12}^{\circ}$  is given by the initial slope of the shear stress ( $\sigma_{12}$ ) versus the engineering shear strain (2 $\epsilon_{12}$ ).



The initial shear modulus is defined as the initial slope of the test curve (remembering that engineering shear strain must be used ( $\gamma_{12}=2\epsilon_{12}$ ),

 $G^{o}_{12} = \sigma_{12} / 2\epsilon_{12} = 60 / (2^*0.0075) = 4.0 \text{ GPa}.$ 

#### 3b. Shear damage properties (cyclic tension test on a ±45° specimen)

The previous cyclic shear test for tensile loading of a  $\pm 45^{\circ}$  coupon is used to extract damage evolution, plasticity and final shear failure data. Shear damage is given by the change in slope of the cyclic modulus G<sub>12i</sub> and plasticity by the growth in  $\epsilon_{ip}$  and each loading cycle i.



Five loading cycles have been performed on the coupon as shown in the next curve. Note that this figure shows test results with, and without, taking account of changes in cross sectional area in the computation of  $\sigma_{12}$ . If these changes can be measured during testing and included then the model calibration will be more accurate. The curve with section variation is used here.



At each cycle the stiffness loss is characterised by the shear modulus reduction. The degree of shear damage  $d_{12}$  is given by the relationship:

$$d_{12}^{i} = 1 - \frac{G_{12}^{i}}{G_{12}^{0}}$$

Shear modulus and damage values for every cycle are summarised in the table below; again using engineering shear strain ( $\gamma_{12}=2\epsilon_{12}$ ) to calculate the G values,

cycle	Shear modulus G <sub>12</sub>	<b>d</b> <sub>12</sub>
0	4.0	0
1	3.914	0.1027
2	3.302	0.2430
3	2.453	0.4376
4	2.255	0.4830
5	2.237	0.4872

This model uses the term Y12 to define how damage is progressing (it is the change of stored elastic energy with damage). The stored energy for a ply is,

$$E_{D} = \frac{1}{2} \underline{\underline{\sigma}} : \underline{\underline{\varepsilon}}^{e}$$
$$= \frac{1}{2} \left[ \frac{\sigma_{11}^{2}}{E_{11}^{0}} - \frac{2\nu_{12}^{0}}{E_{11}^{0}} \sigma_{11} \sigma_{22} + \frac{\langle \sigma_{22} \rangle_{+}^{2}}{E_{22}^{0}(1 - d_{22})} + \frac{\langle \sigma_{22} \rangle_{-}^{2}}{E_{22}^{0}} + \frac{\sigma_{12}^{2}}{G_{12}^{0}(1 - d_{12})} \right]$$

Considering only stored energy for shear (12) the conjugate quantity  $Y_{12}$  is

$$Y_{12} = \frac{\delta E_D}{\delta d_{12}} = \frac{1}{2} \frac{\sigma_{12}^2}{\sigma_{12}^0 (1 - d_{12})^2}$$

From

 $\varepsilon_{12} = \frac{\sigma_{12}}{2G_{12}^o (1 - d_{12})} \qquad > \qquad Y_{12} = \frac{1}{2}G_{12}^0 (2\varepsilon_{12}^{e^i})^2$ 

A similar expression to  $Y_{22}$  could be developed for UD plies where damage will occur in the unreinforced transverse direction; however this is not needed here for the woven fabric. The conjugate force quantity at each cycle (i) is therefore given by,

$$Y_{12}^{i} = \sqrt{\frac{1}{2}G_{12}^{0}(2\mathcal{E}_{12}^{e^{i}})^{2}}$$

From the cyclic test curve and the above expression,

cycle	$oldsymbol{\mathcal{E}}_{12}^{e}$	Yi
0	2.00E-03	0.005656
1	5.10E-03	0.015064
2	9.60E-03	0.028355
3	1.70E-02	0.050212
4	2.45E-02	0.072364
5	2.95E-02	0.087132

It is now possible to plot the evolution of  $Y_{12}$  with damage  $d_{12}$ .

Yi	<b>d</b> <sub>12</sub>
0	0
0.005656	0
0.015064	0.1027
0.028355	0.2430
0.050212	0.4376
0.072364	0.4830
0.087132	0.4872
	Y <sub>i</sub> 0 0.005656 0.015064 0.028355 0.050212 0.072364 0.087132

The damage is initially linear (for small strains and then increases rapidly close to failure), as shown in the adjacent plot. Several options are available in PAM-CRASH to characterise damage evolution; for example, an exponential function, a curve function and the following (original) linear damage function,

$$Y_{12}^{i} = Y_{C} \times d_{12}^{i} + Y_{0}$$

where Yo is the initial constant and Yc is the slope of the linear function. A further parameter YR is used to specify failure (Yo, Yc and YR are data input values for PAM-CRASH shear damage evolution and failure).

Two examples to try and fit the linear function to the test curve are shown in the graph with data in the table below; clearly this is not accurate. For this ductile matrix the exponential or curve function methods would be better.



	Yo	Y <sub>C</sub>	Y <sub>R</sub>
Lin. Function 1	0.005	0.1014	0.05
Lin. Function 2	0.0004	0.1464	0.07
Curve function	Using the data points		0.088
	in the table above		

#### 3c. Shear plasticity properties (Cyclic tension test on a ±45° specimen)

The inelastic deformation is described by a plasticity law which couples transverse (22) and shear (12) strains only. The plastic strain  $p_j$  is the measure of effective plastic strain and the term  $R_j$  is used to determine how the value of  $d_{12}$  affects the yield stress in each cycle.

In this model the terms "effective stress" and "effective strain" are introduced as measures of actual material stress and strain carried by the damaged material. The damage (micro-cracking) reduces the "effective" area of the load carrying material causing effective material stress to be raised and effective material strain to be lowered. Note this terminology is not the same as Von Mises effective stress and strain which is commonly used in plasticity in the literature.

The term  $p_i$  and  $R_i$  are calculated in the following equations:

$$p_{i} = \int_{\varepsilon_{12}^{p'}}^{\varepsilon_{12}^{p'}} 2(1-d_{i})\varepsilon_{12}^{p} \\ P_{j} = \sum_{i=1}^{i=j} p_{i} \\ R_{i} = \frac{\sigma_{12}^{i}}{1-d_{i}} - R_{0}$$
  $\Rightarrow R_{i} = \beta(P_{j})^{m}$  (Eq 1.)

 $1 \le i, j \le$  number of cyclic loads

where  $\epsilon_{12}^{P}$  is the plastic strain at each cycle i, as shown on figure below. The following table gives the plastic strain measured from the cyclic shear test curve and the damage term which are used to calculate pi. According to Equations 1 a plot of  $1-d_{12}$  versus  $2\epsilon_{12}^{P}$  allows the (p<sub>i</sub>) values to be found by integration for each cycle. The values for (P<sub>j</sub>) are then computed from summation of these values. The following curve and table summarise results of this integration and the summation.



cycle	$\boldsymbol{\mathcal{E}}_{12}^{\ p}$	<b>1 - d</b> <sub>12</sub>
0	0	1
1	7.24E-04	0.897295
2	4.90E-03	0.756992
3	1.77E-02	0.562357
4	4.75E-02	0.516965
5	8.45E-02	0.512838



Cycle	<b>p</b> i	Pj	R <sub>i</sub> (MPa)	
0	0	0	0	
1	0.001448	0.001448	0.026362	
2	0.007494	0.008942	0.065272	
3	0.019379	0.028321	0.129727	
4	0.033516	0.061838	0.193748	
5	0.038255	0.100093	0.239731	

Finally, a curve fitting exercise is performed to fit the PAM-CRASH exponential plasticity function (with parameters  $\beta$  and m) to the Ri versus Pi curve. This has produced the following results with the initial plasticity yield stress Ro = 20MPa.



# Part 3: Summary of the Global Ply dataset for elastic, damage, plasticity and failure

For the purpose of this calibration a total ply thickness of 1.0mm is assumed meaning that each ply in the stacked approximation is 0.5mm (Make sure the true value is used in any real composite).

In order to compensate for the halved ply thickness in this idealised model:

- Double the modulus for tension and compression modulus.
- Use unchanged shear modulus (and shear damage/plasticity) for each ply.
- Use a low modulus (say 1GPa) for the transverse direction (to minimise interaction effects).
- Note: Any modifications to ply modulii will correspondingly modify the stress levels; however, damage and failure is always controlled by strain and therefore the approach (to treat a woven composites as two stacked UD plies) is valid.

The following table summarises the data so far for each ply (thickness = 0.5mm) in the idealised woven composites.

Inplane Tension	Inplane Compression		
E <sub>1</sub> <sup>0t</sup> = (2*67.5)=135 GPa	$E_1^{0c}$ = (2*69,0)=138 GPa		
$E_2^{0t} = 1.0 \text{ GPa}$	$\gamma$ = 0.17		
$v_{12}^0 = 0.33$	$\mathcal{E}_i^{fc} = 0.0104$		
$\mathcal{E}_i^{ft} = 0.013$	$\mathcal{E}_{u}^{fc}=0.0105$		
$\mathcal{E}_{u}^{ft}=$ 0.0131	$d_{u}^{fc} = 1.0$		
$d_{u}^{ft} = 1.0$			

Table 1: Inplane stiffness/failure data

For the shear the following data/options were determined (to be used for each ply):

Stiffness	G <sup>0</sup> <sub>12</sub> = 4.0 GPa				
Damage	Yo Yc		YR		
Lin. Function 1	0.005	0.1014	0.05		
Lin. Function 2	0.0004	0.1464	0.07		
Curve function	Using the Y12-d12 data points 0.089				
Plasticity	$R(P_i) = 0.7986 P_i^{0.5166}$				
	$\Rightarrow$ $R_0$ = 20MPa, $\beta$ = 0.7986, m = 0.5166				

Table 2: Shear stiffness, damage and plasticity data

#### Part 4: Checking the input with simulation results

#### Simulation results

#### Fibre tension (elastic without and with failure)

Using dataset: Ply1\_TensionX\_ElasticFibre.pc (for no failure) Ply1\_TensionX\_ElasticFibreFailure.pc (for fibre failure)

Positive x-velocity is applied to nodes 2,3 (0.1mm/sec) (= Case 1, Pg 2)..

#### Fibre tension (for the failure case)

The shell element time history plot Comp. Aux4 (fibre stress) against Aux1 (fibre strain) is plotted for the fibre direction ply. For a strain of 0.01 the corresponding fibre direction stress is  $\approx$ 1.35GPa; note:

 This stress is (≈ correctly) double that of the test value (700N/mm2 at 0.01 strain) since the equivalent ply thickness is half of the true woven ply. The difference is due to the small contribution from the transverse direction in the second ply; calibration could be done to correct this.



- 2. The failure data  $\varepsilon_i^{ft} = 0.013$ ,  $\varepsilon_u^{ft} = 0.0131$  and  $d_u^{ft} = 1.0$  is imposed. In this case tensile fibre failure is initiated at the required 1.3% strain and full damage occurs (d=1.0).
- 3. If a residual damage is required use d<1.0. E.g. for d=0.3 only 30% of damage occurs (Edamage = 0.7 \* Eo) and the stress <u>will remain constant</u> after this damage state is reached.

#### **Results: fibre compression**

Using dataset: Ply1\_CompressionX\_ElasticFibre.pc (for no failure) Ply1\_CompressionX\_ElasticFibreFailure.pc (for fibre failure)

Negative x-velocity (=-0.1mm/sec) is applied to nodes 2,3..

#### Fibre compression (for the failure case)

- The nonlinear form of the compression fibre stress (Aux 4) versus fibre strain (Aux 1) is evident due to the factor γ = 0.17.
- Stress in the fibre ply (x-direction) is approximately twice the test value due to the previously mentioned reason; for example, at fibre strain 0.09, the simulation stress is 1.02kN compared to test 0.54kN.
- The failure data  $\varepsilon_i^{fc} = 0.010$ ,  $\varepsilon_u^{fc} = 0.011$ and  $d_u^{fc} = 1.0$  is imposed. Failure is initiated and completed, as expected, with total damage due to d=1.0.



#### Transverse direction (= Case 2, Pg 2)

Since this composite has a balanced fabric the second ply transverse direction will have the same properties as the fibre direction calibrated above. This is assured in the dataset using 2 layers for the model with identical properties for layer 1 (in the 0°) and layer 2 (in the 90°).

**Shear** (for the elastic case using dataset - Ply1\_ShearXY\_Elastic.pc)

The single element test case is loaded in the positive x and negative y directions to impose pure shear loading (= Case 3, Pg 2). The fibre directions are set to  $\pm 45^{\circ}$  with respect to the x-direction.

A time history plot of shear stress  $\sigma_{12}$ (Aux6) against shear strain  $\epsilon_{12}$  (Aux3) is shown. At 0.0075 shear strain the shear stress is 60MPa; which corresponds to the value of the initial slope of the experimental shear stress versus shear strain curve.

![](_page_14_Figure_6.jpeg)

Shear (for the damage with failure plus plasticity)

Shear damage can be treated using the linear damage function, an exponential function or the curve function; ultimate shear failure is specified by the value of YR. The previous table for shear damage evolution and failure is repeated below with the three options (1, 2, 3) evaluated here to compute shear damage. In each case the previously determined plasticity data is used.

		Shear damage data		Plasticity data			
Option	Damage function	Yo	Yc	YR	Ro	β	m
1	Lin. Function 1	0.005	0.1014	0.05	20 MPa	0.7986	0.5166
2	Lin. Function 2	0.0004	0.1464	0.07	20	0.7986	0.5166
3	Curve function	using the data points in the Y12-D12 table		0.089	20	0.7986	0.5166

#### The three supplied datasets for the above cases are:

- 1. Ply1\_ShearXY\_ElasticDamageFailure\_Option1\_Plastic.pc
- 2. Ply1\_ShearXY\_ElasticDamageFailure\_Option2\_Plastic.pc
- 3. Ply1\_ShearXY\_ElasticDamageFailure\_Option3\_Plastic.pc

**Using the linear shear function** (options 1 and 2): For some semi-brittle materials the linear fit may be satisfactory; but in this case the fit is poor, especially to describe the rapid damage growth at large shear strains. The following curves illustrate the poor fit of the linear function to the test (damage) curve and the correspondingly poor correlation of the single element analysis to the test shear stress-strain curve.

![](_page_15_Figure_1.jpeg)

#### Using the curve shear function (option 3)

In PAM-CRASH (version V2008+) exponential and curve descriptions for shear and transverse damage evolution are available. In the Option 3 dataset the 'Linear' parameters for Yo, Yo' are removed and the variable ISH is set to 2. A curve description of Yi against d12 is used with the previously determined data (note the 0,0 start point) in an auxiliary curve; set this curve number to the parameter ICURV1 in the ply data. The ultimate shear strain parameter YR is set to 0.089.

From the results a plot of shear stress (Aux 6) against shear strain (Aux 3) shows a good

![](_page_15_Figure_5.jpeg)

agreement with the test curve for both shape and failure; although some improvements using more data points could help to smooth the shape, especially at shear strain 0.04.

#### Cyclic shear loading

Using shear damage (option 3) and the dataset Ply1\_ShearXY\_ElasticDamageFailure\_Option3 \_Plastic\_Cyclic.pc

The adjacent plot shows cyclic (velocity) loading of the single element test case. The change in slope of the unloading curve represents damaged shear modulus. Also, the inelastic (permanent) plastic strains are evident.

![](_page_15_Figure_10.jpeg)

#### Part 5: Alternative options for damage and failure

#### Damage curve functions

Different methods can be used to define the form of the damage functions; namely, Linear, Exponential or Curve. For most composites an exponential or Curve function will be needed to reasonably describe the damage function evolution.

![](_page_16_Figure_4.jpeg)

#### Superimposed failure criteria

For fibre and matrix damage the Global ply model has so far been used. However, it is also possible to superimpose a classical failure criteria such as Tsai-Wu, Max. stress, etc.

Set IFAIL\_INP=1 and choose the failure criteria with flag FAILTYP. Depending on the selected failure criteria additional failure information is required. If the state of stress or strain reaches the failure criteria the element will be eliminated (for FAILDAM = 1). In the materials cards the IFAIL option must also be set.

![](_page_16_Figure_8.jpeg)

### Part 6: Specific information for woven reinforcement (Mat 131 ply type 7)

Ply Creation/Editing

The data shown is typical information for ply type 7. Some points to note are:

- 1. The structure and general information required is similar to ply type 1.
- 2. The two main fibre directions are assumed to be orthogonal.
- Tension and compression information is provided for the main fibre direction (E01, E0c1) and the second fibre direction (E02, E0c2).

![](_page_16_Figure_14.jpeg)

4. For tension fibre failure driving force values YIIC, Y110 and Y11R are used, for compression YIICC, Y11c0 and Y11cR are used. Note that currently this information is applied to both reinforcement directions, so strictly the fabric should be balanced (i.e. E01 = E02 and E0c1 = E0c2).

5. Strain rate can be applied.